

Internal Consistency Reliability

- Split-Half reliability
- Cronbach's alpha Tau equivalent
- Spearman-Brown Prophesy formula Longer is more reliable

Test-Retest Reliability

- administered at two time points

 - Need 3 or more time points to separate error from Assumes no learning, practice, or fatigue
- Probably the most important form of
- reliability for psychological inference

Interrater Reliability

- Could be estimated as correlation between two raters or alpha for 2 or more raters
- Typically estimated using intra-class
- Shrout & Fleiss (1979); McGraw & Wong

Interrater Reliability

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Intraclass Correlations: Uses in Assessing Rater Reliability

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peficients often take the form of intraclass correlation, fe, guidelines are given for choosing among six differen correlation for reliability studies in which a tagets are att to the choice of far coefficient are the appropriate reliability study and the applications to be made of the donet sizerals for each of the forms are reviewed.

Intraclass Correlations

- Variables that share a metric and variance
- Height and Weight are different classes of
- There is only 1 Interclass correlation
- When interested in the relationship between variables of a common class, use an Intraclass Correlation Coefficient.

Intraclass Correlations

An ICC estimates the reliability ratio directly

Recall that... $r_{xx} = \frac{\sigma_t^2}{\sigma_o^2} = \frac{\sigma_t^2}{\sigma_t^2 + \sigma_e^2}$ An ICC is estimated as the ratio of variances: $ICC = \frac{Var(subjects)}{Var(subjects) + Var(error)}$

Intraclass Correlations

- The variance estimates used to compute this ratio are typically computed using ANOVA
 - Person x Rater desig
 - In reliability theory, classes are persons between person variance
 - The variance within persons due to rater differences is the error

Fxai	Intra	class	S Cor	relati	ons	
	Persons	Rater1	Rater2	Rater3	Rater4	I A
	1	9	2/\	5	8	$ / \rangle$
	2		1	3	2	
	3	8	/4	6	8	
	4	7	/ 1	2	6	
	5	10	5	6	9	
	6	6	2	4	7	6
						9

Intraclass Correlatior	າຮ				
 3 sources of variance in the design persons, raters, & residual error No replications so the Rater x Rate interaction is confounded with the 	n: ee errc	r			
ANOVA results Source df MS					
Between Persons	5	11.24			
Within Persons	18	6.26			
Between Raters	3	32.49			
Residual Error	15	1.02			

Intraclass Correlations

- Based on this rating design, Shrout & Fleiss defined three ICCs
 - ICC(1,k) Random set of people, random set of raters, nested design, rater for each person is selected at random
 - ICC(2,k) Random set of people, random set of raters, crossed design
 - ICC(3,k) Random set of people, FIXED set of raters, crossed design

ICC(1,k)

- A set of raters provide ratings on a different sets of persons. No two raters provides ratings for the same person
- In this case, persons are nested within raters.
- Can't separate the rater variance from the error variance
- k refers to the number of judges that will actually be used to get the ratings in the decision making context

ICC(1,k)

$$ICC(1,k) = \frac{\sigma_p^2}{\sigma_p^2 + \frac{\sigma_w^2}{k}}$$
• Agreement for the average of k ratings
• We'll worry about estimating these
"components of variance" later

ICC(2,k)

$$ICC(2,k) = \frac{\sigma_p^2}{\sigma_p^2 + \frac{(\sigma_r^2 + \sigma_e^2)}{k}}$$
• Because raters are crossed with ratees you can get a separate rater main effect.
• Agreement for the average ratings across a set of random raters

ICC(3,k)

$$ICC(3,k) = \frac{\sigma_p^2}{\sigma_p^2 + \frac{(\sigma_e^2)}{k}}$$
Raters are "fixed" so you get to drop their variance from the denomenator

 Consistency/reliability of the average rating across a set of fixed raters

ICC	Estimate
ICC(1,1)	0.17
ICC(2,1)	0.29
ICC(3,1)	0.71
ICC(1,4)	0.44
ICC(2,4)	0.62
ICC(3,4)	0.91

ICCs in SPSS						
For SPSS, you must choos (1) An ANOVA Model (2) A Type of ICC	30: 					
ANOVA Model						
One way Random Effects	ICC(1,1)					
TYPE:	Consistency	Absolute Agreement				
Two way Random Effects		ICC(2,1) "ICC(AGREEMENT)"				
Two way Mixed Model : Raters Fixed Patients Random	ICC(3,1) "ICC(CONSISTENCY)"					

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		000	D A	163	41. 3	0	
	patients	rster1	rate/2	rater3	raber4	ver.	T
- 1	1	9	- 2	6	8	1	1
2	2	6	1	3	2		
3	3	8	4	Б.	8		
4	4	7	2	2	6		-
	5	10	5	- 9-	9		+-
7							-
							-
10							
100							





ICCs in SPSS						
	Choose Reliability Analysis: Statistics					
Analysis under the	Descriptives for Item Scale Scale	Inter-Item Correlations Contin Covariances Help	2			
statistics tab	Summaries Means Summarices Covariances Copelations	ANOVA Table © Mone © E test © Friedman chi-tguare © Codyran chi-square				
	Hotelling's T-square Intraclass correlation coe Model: Two-Way Rando Confidence interval: 95	Tugey's test of additivity flicient Tyget: Absolute Agreemer Tyget: 0				

ICCs in SPSS
Output
RELIABILITY ANALYSIS
Intraclass Correlation Coefficient
• Two-way Random Effect Model (Absolute Agreement Definition):
People and Measure Effect Random
Single Measure Intraclass Correlation = .2898*
<pre>95.00% C.I.: Lower = .0188 Upper = .7611</pre>
F = 11.02 DF = (5,15.0) Sig. = .0001 (Test Value = .00)
Average Measure Intraclass Correlation = .6201
<pre>95.00% C.I.: Lower = .0394 Upper = .9286</pre>
<pre>F = 11.0272 DF = (5,15.0) Sig. = .0001 (Test Value = .00)</pre>
Reliability Coefficients
• N of Cases = 6.0 N of Items = 4







Agreement vs. Reliability

- Reliability/correlation is based on covariance and not the actual value of the two variables
- If one rater is more lenient than another but they rank the candidates the same, then the reliability will be very high
- Agreement requires absolute consistency.

Agreement vs. Reliability

- Interrater Reliabilit
 - "Degree to which the ratings of different judges are proportional when expressed as deviations from their means" (Tinsley & Weiss, 1975, p. 359)
 Used when interest is in the relative ordering of the
 - ratings
- Interrater Agreement
- "Extent to which the different judges tend to make exactly the same judgments about the rated subject" (T&W, p. 359)
 Used when the absolute value of the ratings matters "

Agreement Indices

- Percent agreement
- What percent of the total ratings are exactly the same?
- Cohen's Kappa
- Percent agreement corrected for the probability of chance agreement
- r_{wg} agreement when rating a single stimulus (e.g., a supervisor, community, or clinician).



Kappa

- Typically used to assess interrater agreement
- Designed for categorical judgments (finishing places, disease states)
- Corrects for chance agreements due to limited number of rating scales
 - P_A = Proportion Agreement
 - P_c = expected agreement by chance
- 0 1; usually a bit lower than reliability 29

 $1 - p_{c}$



Kappa Standards

- Kappa > .8 = good agreement
- .67 <kappa <.8 "tentative conclusions"
 Carletta '96
- As with everything...it depends
- For more than 2 raters...
 Average pairwise kappas

Kappa Problems



Kappa Problems

Departures from symmetry in the contingency tables (i.e., prevalence and bias) affect the magnitude of kappa.
 Unbalanced agreement reduces kappa
 Unbalanced discrement increases kappa

r_{wg}

- Based on Finn's (1970) index of agreement
- Rwj is used to assess agreement when multple raters rate a single stimulus
- When there is no variation in the stimuli you can't examine the agreement of ratings over different stimuli

r_{we}

- Could use the standard deviation of the ratings
- Like percent agreement...does account for chance
- r_{wg} references the observed standard deviation in ratings to the expected standard deviation if the ratings are random

 Compares observed variance in ratings to the variance in ratings if ratings were random

$$r_{wg} = 1 - \left| \frac{S_r^2}{\sigma_{EU}^2} \right|$$
; where $\sigma_{EU}^2 = (A^2 - 1)/12$
A is the No. of scale point

- Standard assumption is a uniform distribution over the ratings scale range
- .80 .85 is a reasonable standard