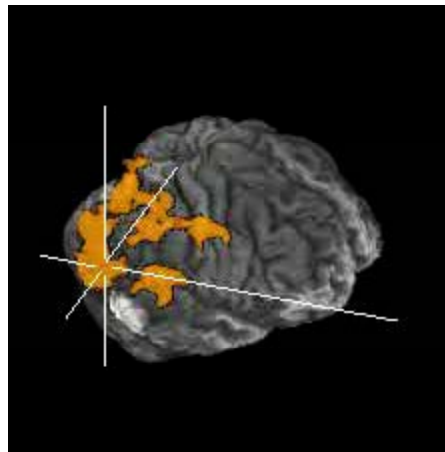


fMRI Block Design and Data Analysis

David C. Zhu, Ph.D.

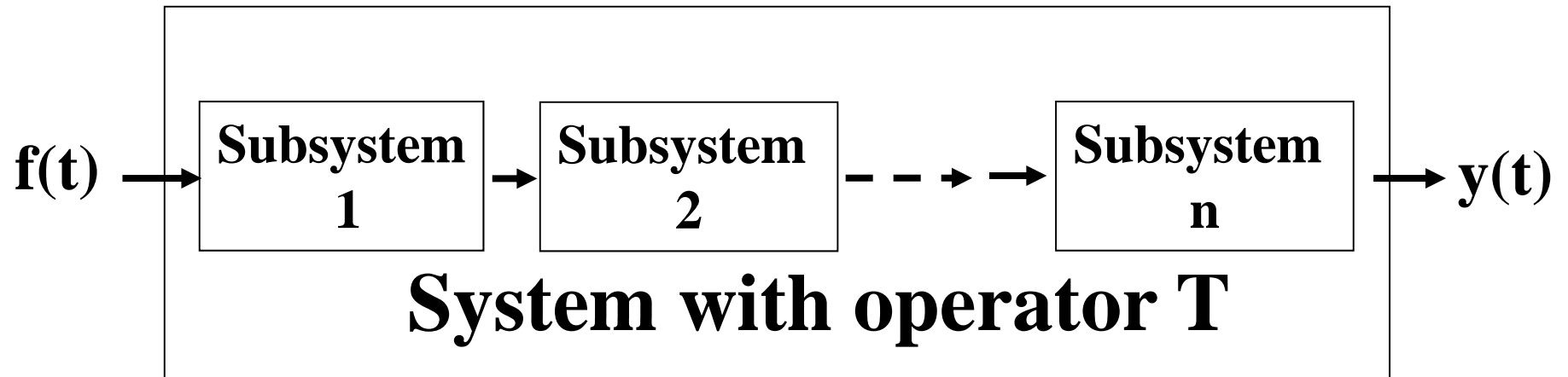
Cognitive Imaging Research Center

Departments of Psychology and Radiology



Reading materials

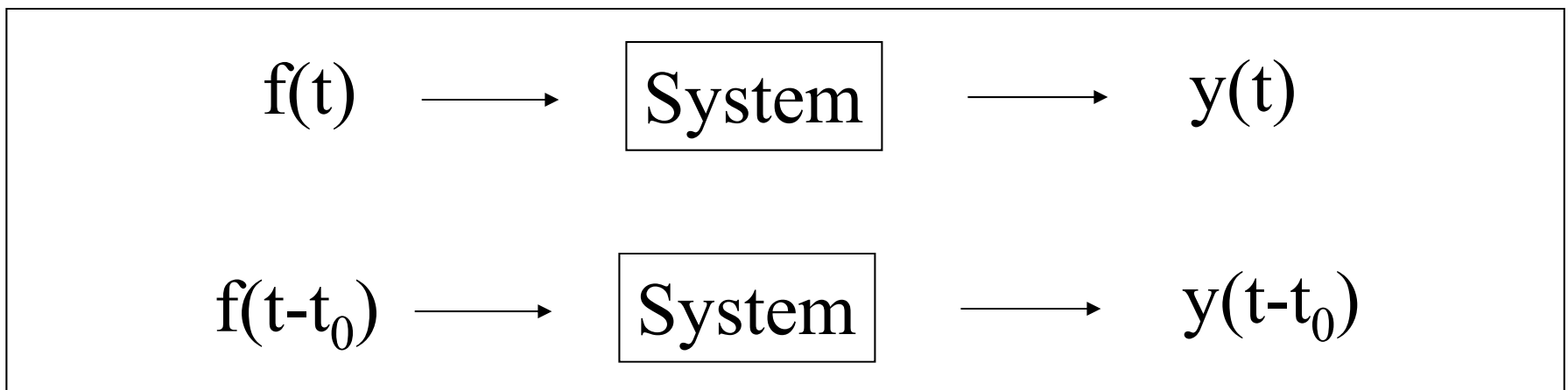
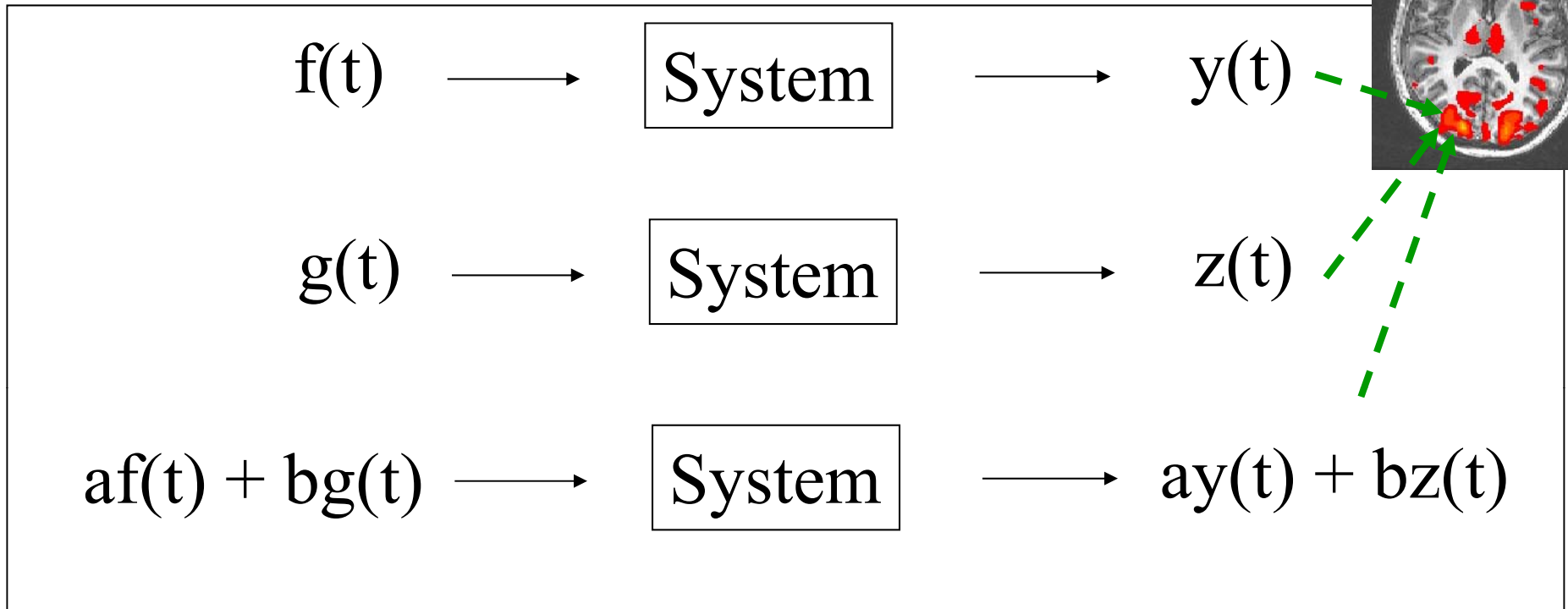
Henderson JM, Larson CL, Zhu DC. Cortical activation to indoor versus outdoor scenes: an fMRI study. *Exp Brain Res.* 2007;179:75-84.



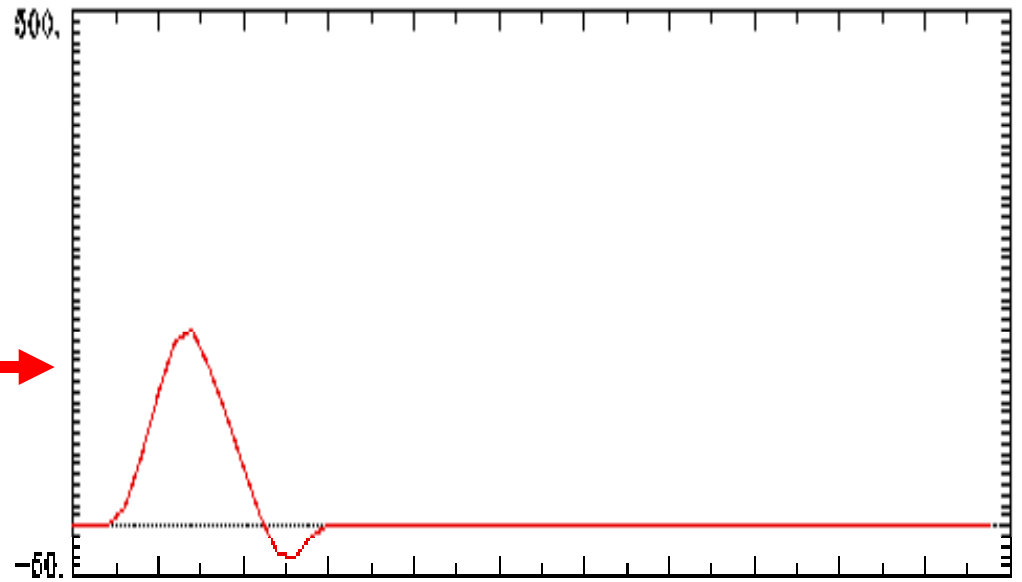
$$y(t) = T\{f(t)\}$$

-
- (1) Find T \Rightarrow Event-related design
 - (2) Assume $T' = T$ based on some model
 Find expected $y'(t) = T'\{f(t)\}$
 Compare $y(t)$ and $y'(t)$
 \Rightarrow Block related design

Linear System



Present for 2 seconds

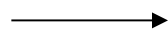


impulse



impulse response

$\delta(t)$

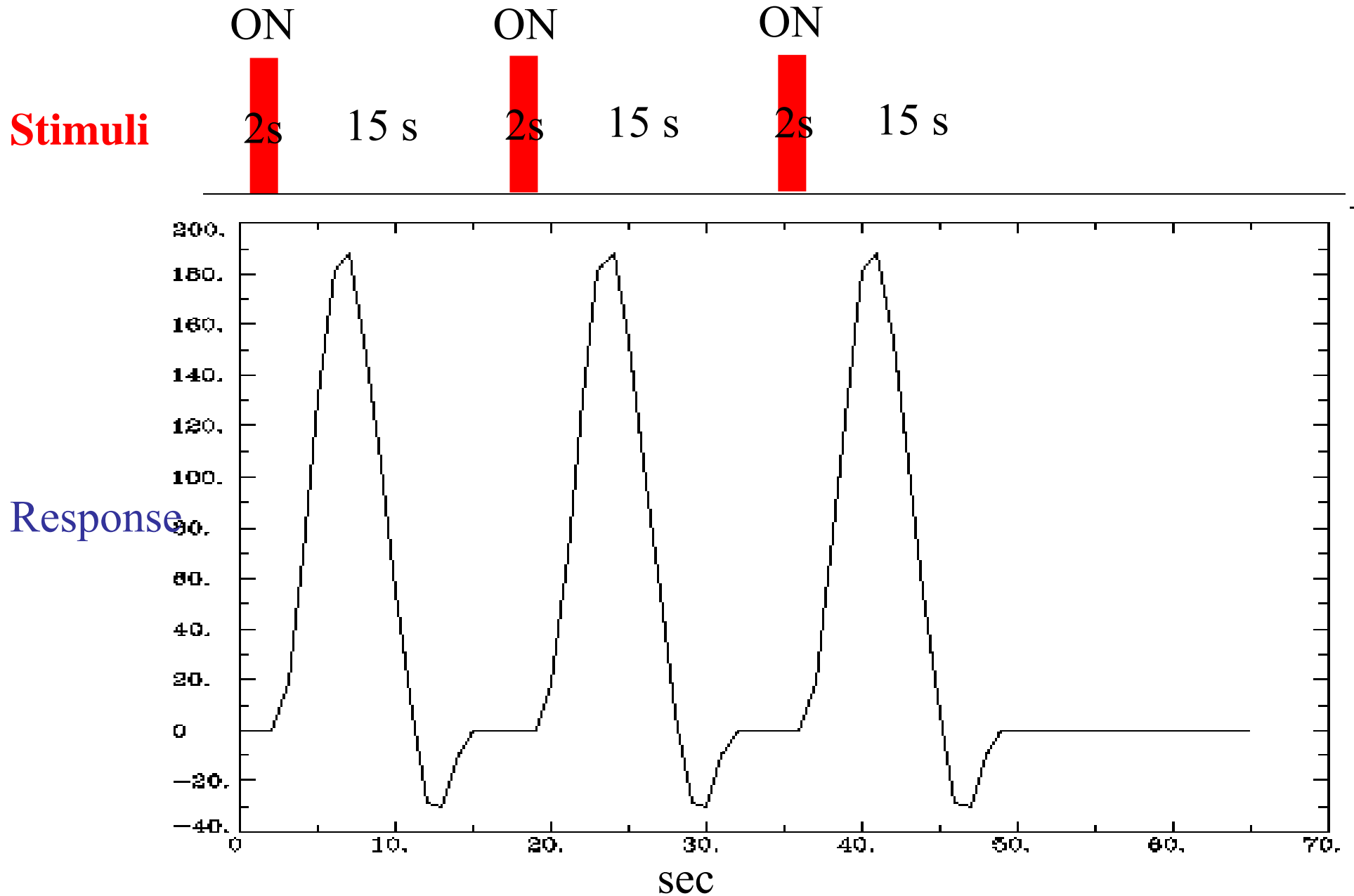


System

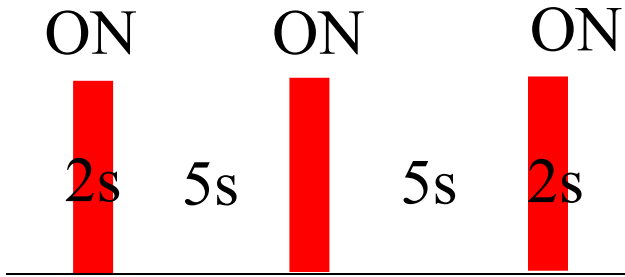


$h(t)$

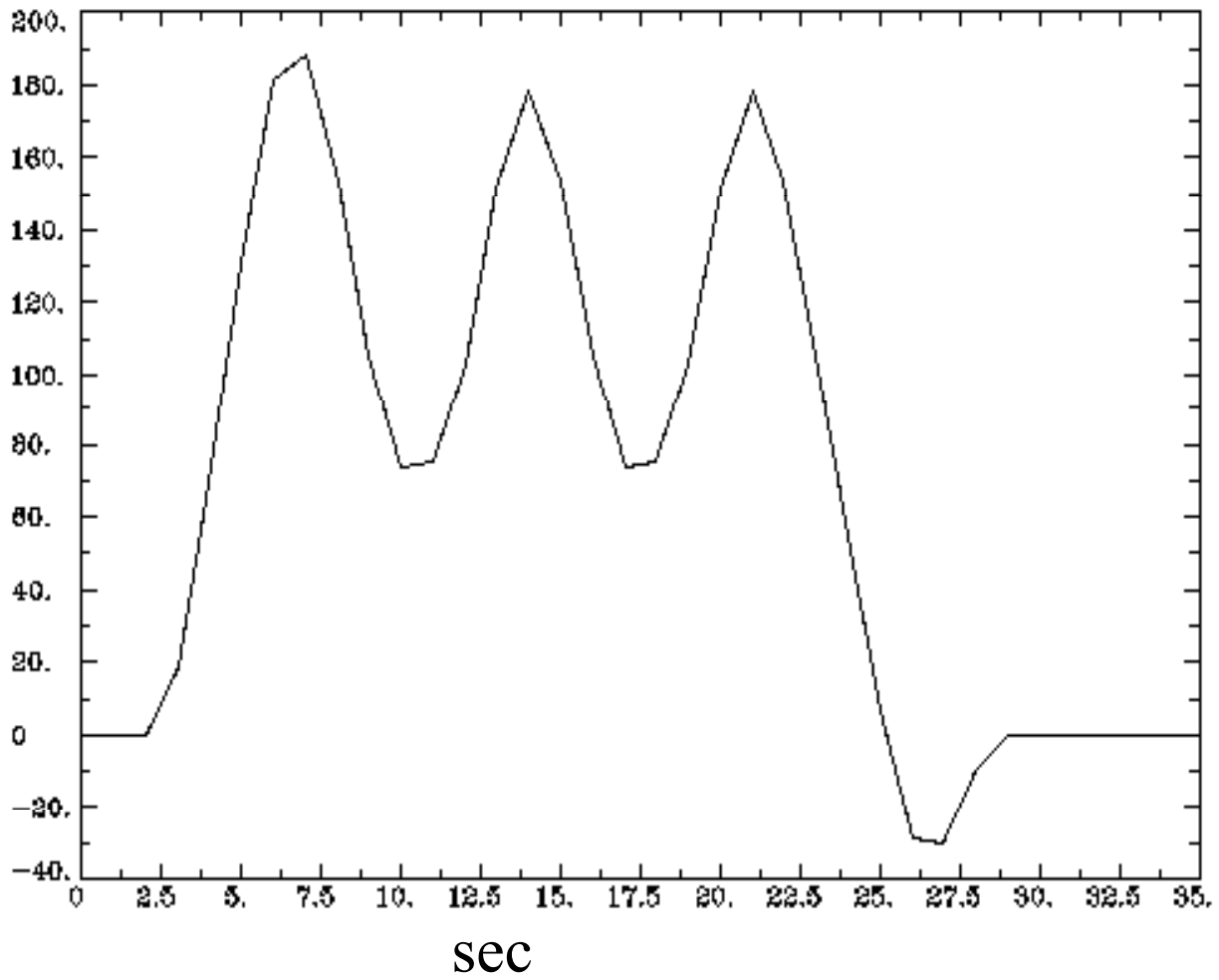
Traditional (Slow) Event Related Design



Stimuli

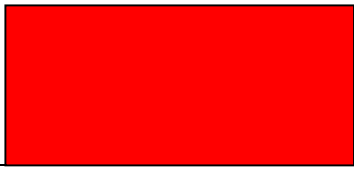


Response

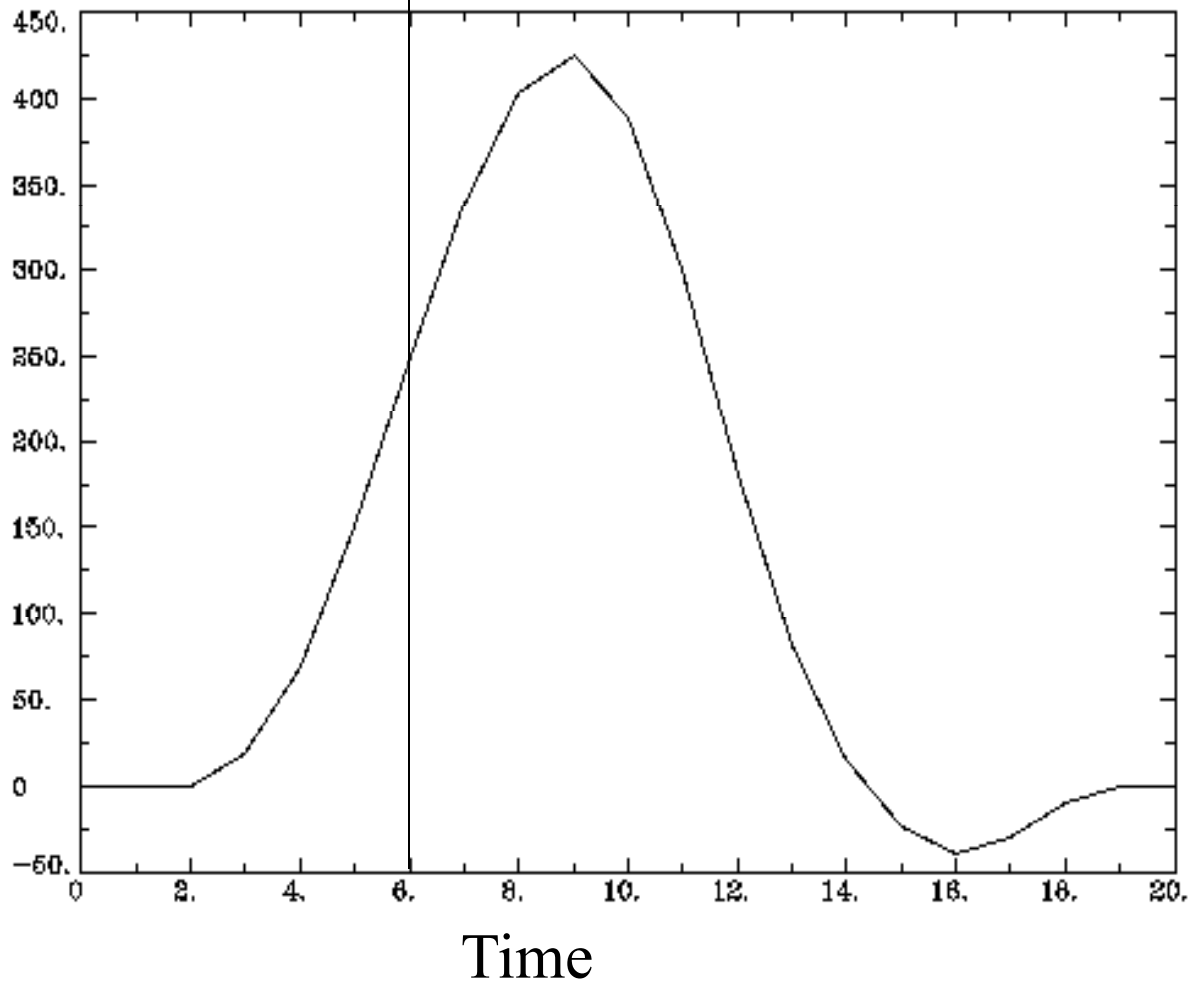


Stimuli

ON

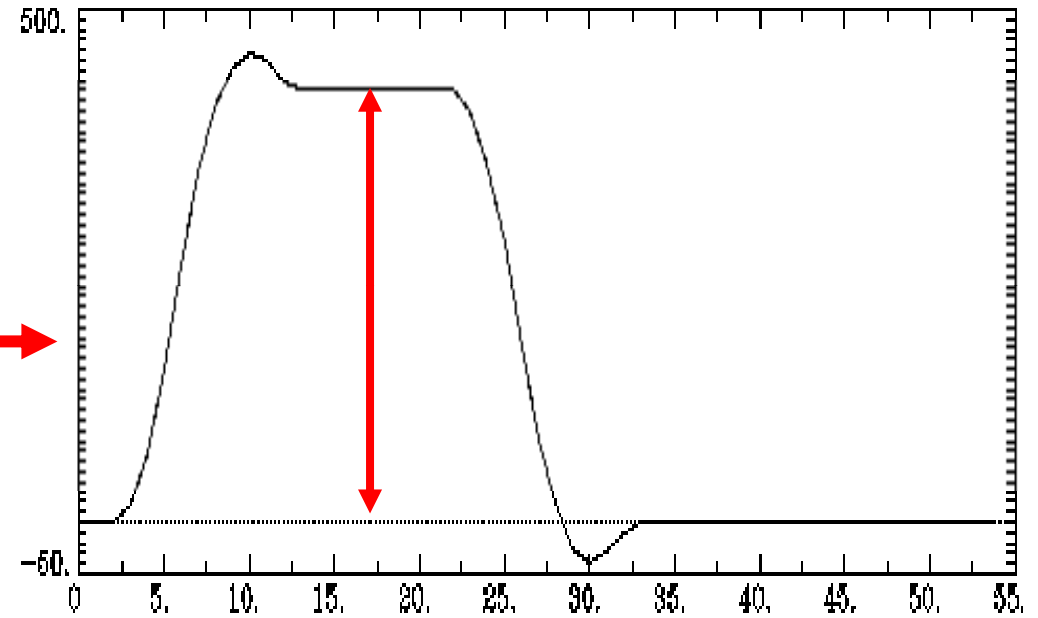


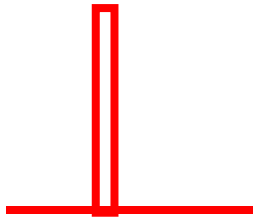
Response



Block Design

Present 10 pictures
With 2 seconds each



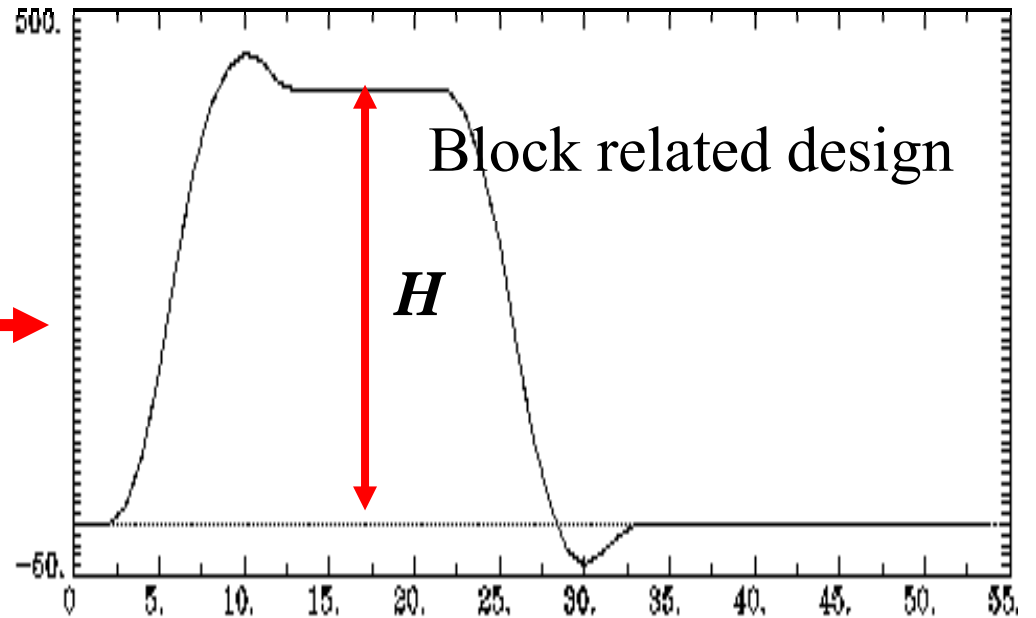
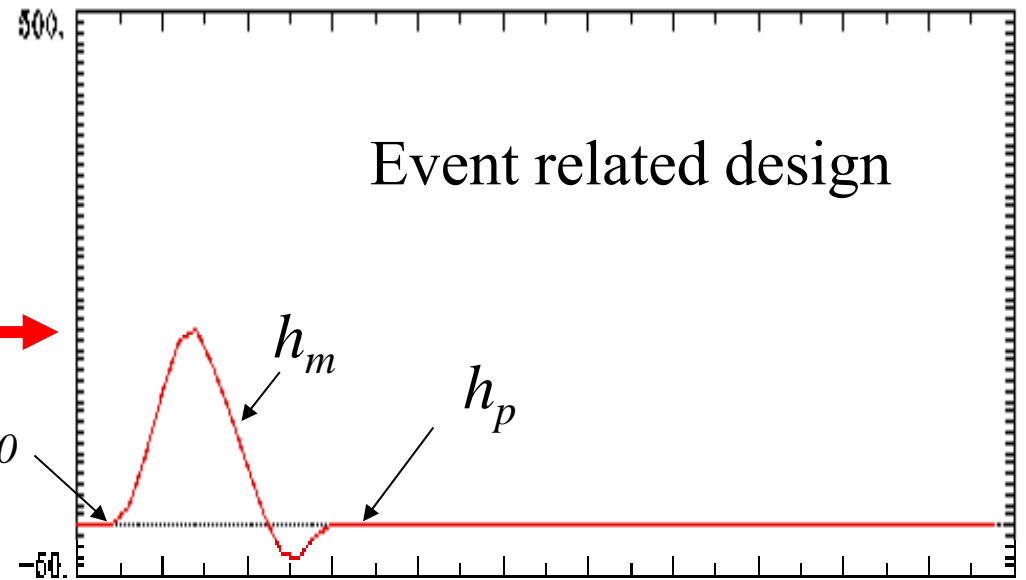
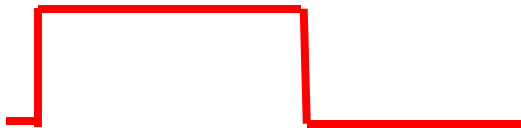


Present for 2 seconds

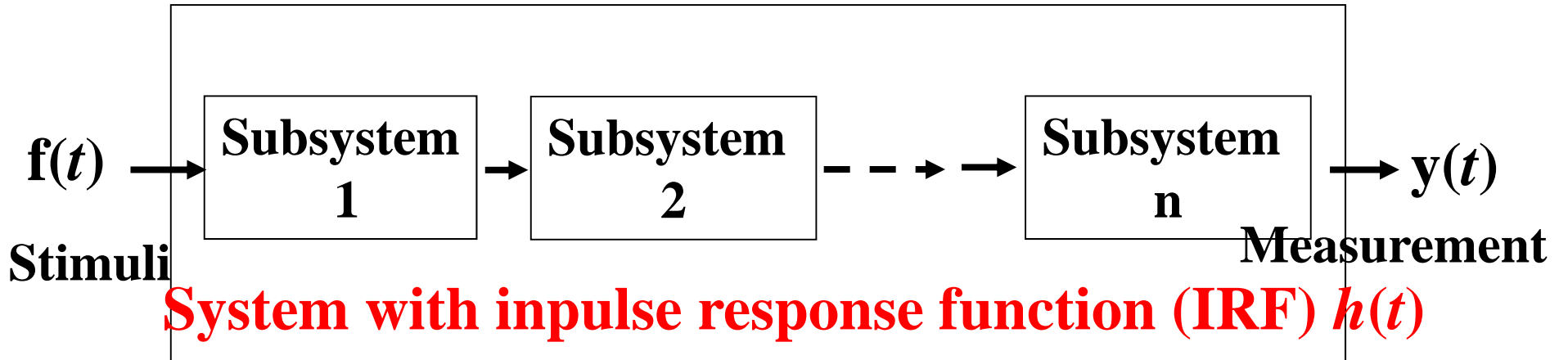


$$H \approx \sum_{m=0}^p h_m$$

Present 10 pictures
With 2 seconds each



Modeling of fMRI



deconvolution

$$y(t) = f(t) \otimes h(t)$$
$$= \int_0^t f(\tau) h(t - \tau) d\tau$$

$h(t)$

Continuous: $y(t) = f(t) \otimes h(t) = \int_0^t f(\tau)h(t - \tau)d\tau$

Discrete times: $y(n\Delta t) = \sum_{m=0}^n f(m\Delta t)h(n\Delta t - m\Delta t)\Delta t$

In short hand,

$$\begin{aligned} y_n &= \sum_{m=0}^n f_m h_{n-m} \\ &= \sum_{m=0}^n f_{n-m} h_m \end{aligned}$$

Assume $h_m = 0$ for $n \geq p$, then

$$y_n = \sum_{m=0}^p f_{n-m} h_m$$

Using the matrix notation,

$$\mathbf{Z} = \begin{bmatrix} \mathbf{Z}_p \\ \mathbf{Z}_{p+1} \\ \cdot \\ \cdot \\ \cdot \\ \mathbf{Z}_{N-1} \end{bmatrix}, \quad \mathbf{X} = \begin{bmatrix} 1 & p & f_p & \cdots & f_0 \\ 1 & p+1 & f_{p+1} & \cdots & f_1 \\ \cdot & \cdot & \cdot & \cdot & \cdot \\ \cdot & \cdot & \cdot & \cdot & \cdot \\ \cdot & \cdot & \cdot & \cdot & \cdot \\ 1 & N-1 & f_{N-1} & \ddots & f_{N-p-1} \end{bmatrix}$$

$$\boldsymbol{\beta} = \begin{bmatrix} \beta_0 \\ \beta_1 \\ h_0 \\ \cdot \\ \cdot \\ \cdot \\ h_p \end{bmatrix} \quad \boldsymbol{\varepsilon} = \begin{bmatrix} \varepsilon_p \\ \varepsilon_{p+1} \\ \cdot \\ \cdot \\ \cdot \\ \varepsilon_{N-1} \end{bmatrix}$$

$$Z_n = k \underbrace{\sum_{m=0}^p f_{n-m} h_m}_{y_n} + \varepsilon_n$$

measurement Error

Including constant baseline + linear trend, the MR signal measured

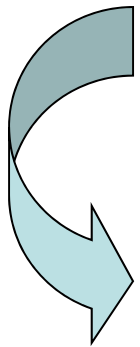
$$Z_n = y_n + \beta_0 + \beta_1 n + \varepsilon_n$$

$$= \beta_0 + \beta_1 n + h_0 f_n + h_1 f_{n-1} + \dots + h_p f_{n-p} + \varepsilon_n$$

For $n = p, p+1, \dots, N-1$

$$Z_n = \beta_0 + \beta_1 n + k y_n + \varepsilon_n$$

For $n = 0, 1, \dots, N-1$



Using the matrix notation,

$$Z = \begin{bmatrix} Z_0 \\ Z_1 \\ \cdot \\ \cdot \\ \cdot \\ Z_{N-1} \end{bmatrix}, \quad X = \begin{bmatrix} 1 & 0 & y_0 \\ 1 & 1 & y_1 \\ \cdot & \cdot & \cdot \\ \cdot & \cdot & \cdot \\ \cdot & \cdot & \cdot \\ 1 & N-1 & y_{N-p-1} \end{bmatrix},$$

$$\beta = \begin{bmatrix} \beta_0 \\ \beta_1 \\ k \end{bmatrix}$$

$$\varepsilon = \begin{bmatrix} \varepsilon_0 \\ \varepsilon_1 \\ \cdot \\ \cdot \\ \cdot \\ \varepsilon_{N-1} \end{bmatrix}$$

$$\mathbf{Z} = \mathbf{X} \boldsymbol{\beta} + \boldsymbol{\varepsilon}$$

The MR signal intensity at a voxel from a 7-min run

Error term

Baseline signal + linear trend + IRF

The design matrix (when the stimulus ON and OFF)

k

$$\hat{\boldsymbol{\beta}} = \begin{bmatrix} \hat{\beta}_0 \\ \hat{\beta}_1 \\ \hat{k} \end{bmatrix} = (\mathbf{X}^t \mathbf{X})^{-1} \mathbf{X}^t \mathbf{Z}$$

\otimes

$h(t)$

Model

$$y(t) = f(t) \otimes h(t)$$

$$y'(t) = f(t) \otimes h'(t) \leftarrow \text{Model}$$

if $h(t) = kh'(t)$

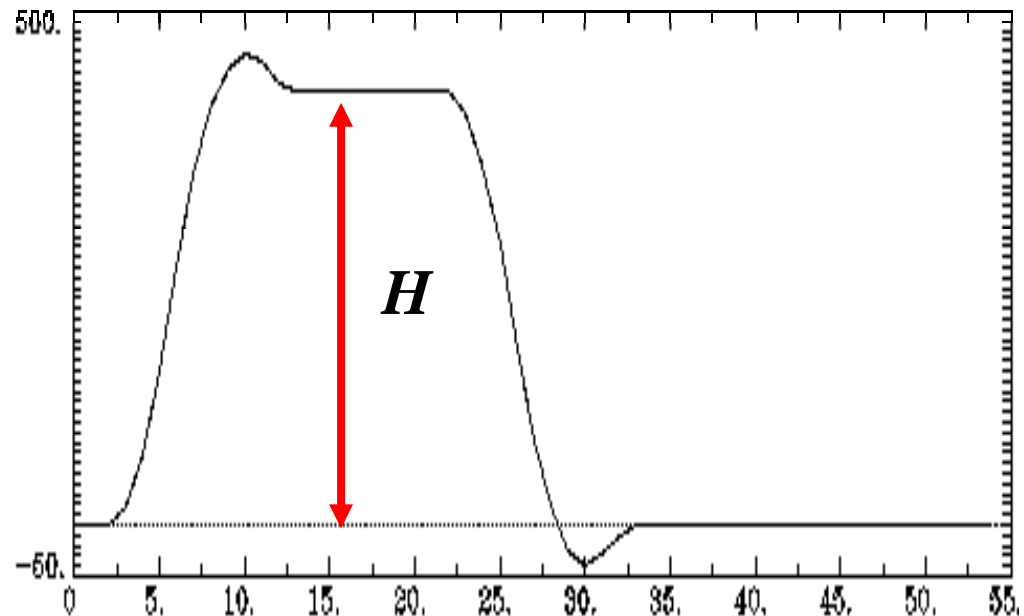
then $y(t) = ky'(t)$

In AFNI, gamma functions:

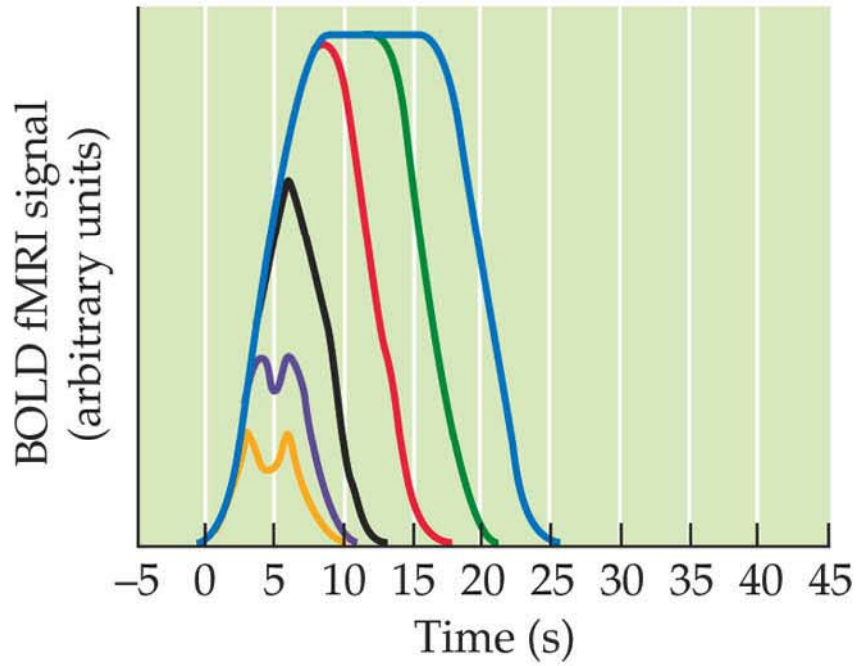
- (1) Default: Cox special
- (2) Mark Cohen

% signal change

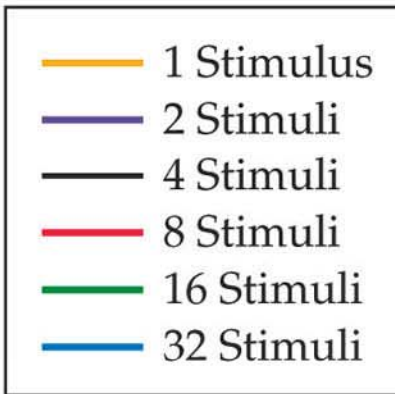
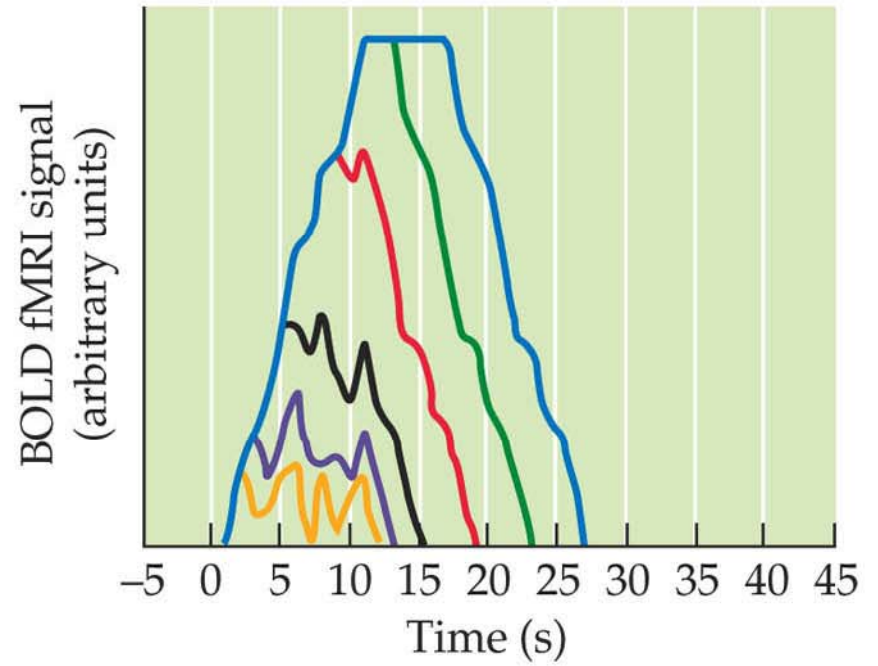
$$= \frac{\hat{k}H}{\hat{\beta}_0}$$



(C)



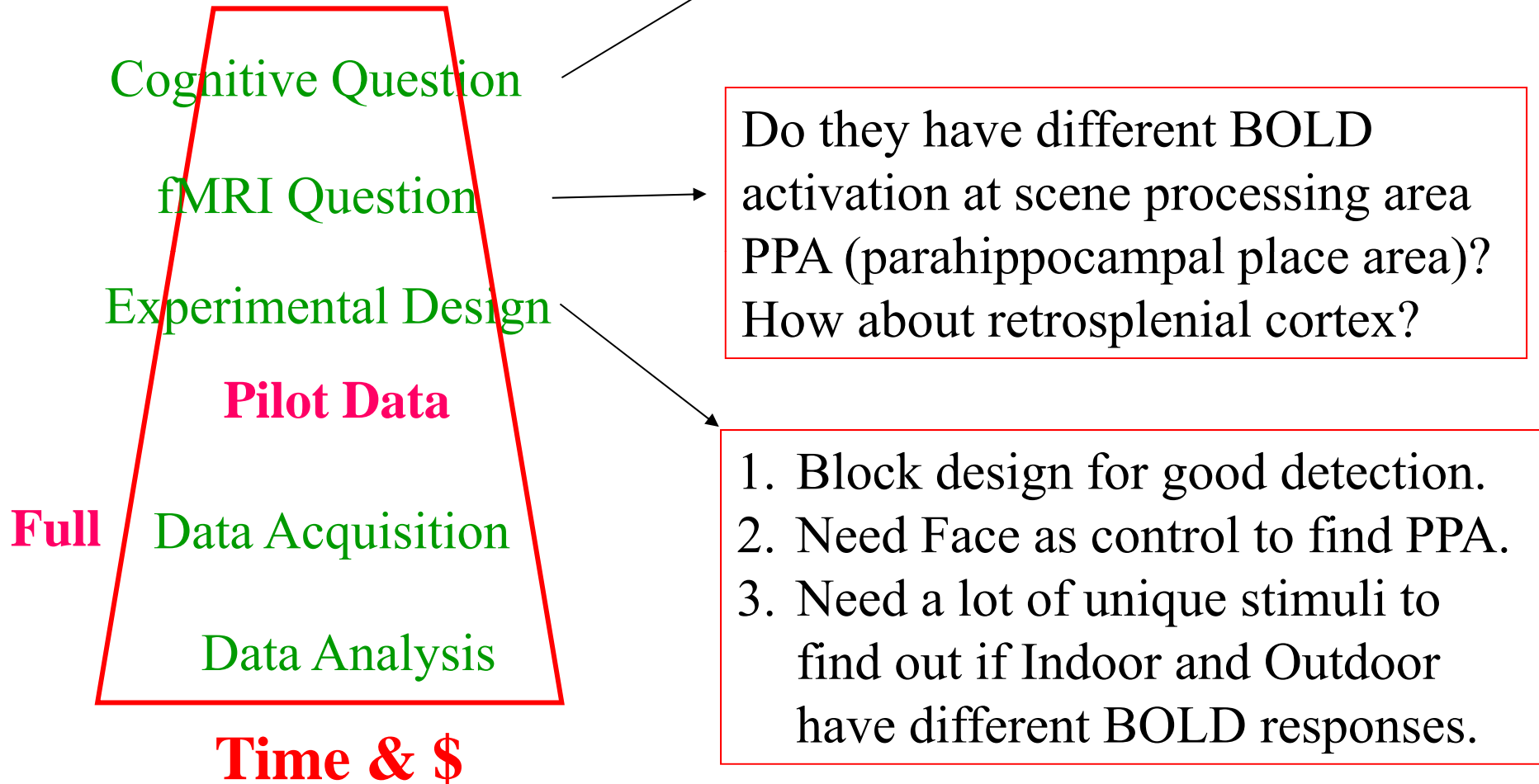
(D)



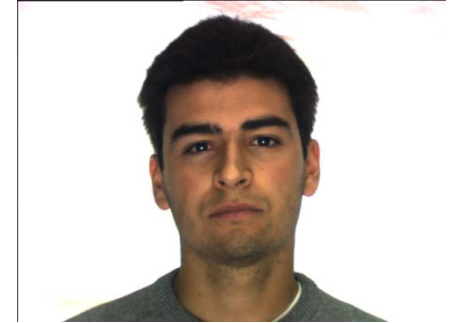
Example

Henderson JM, Larson CL, Zhu DC. Cortical activation to indoor versus outdoor scenes: an fMRI study. *Exp Brain Res.* 2007;179:75-84.

Engineering Process



160 unique faces



160 unique indoor pictures



160 unique outdoor pictures



Detailed Design

160 neutral faces, 160 indoor pictures and 160 outdoor pictures.
No pictures will be repeated.

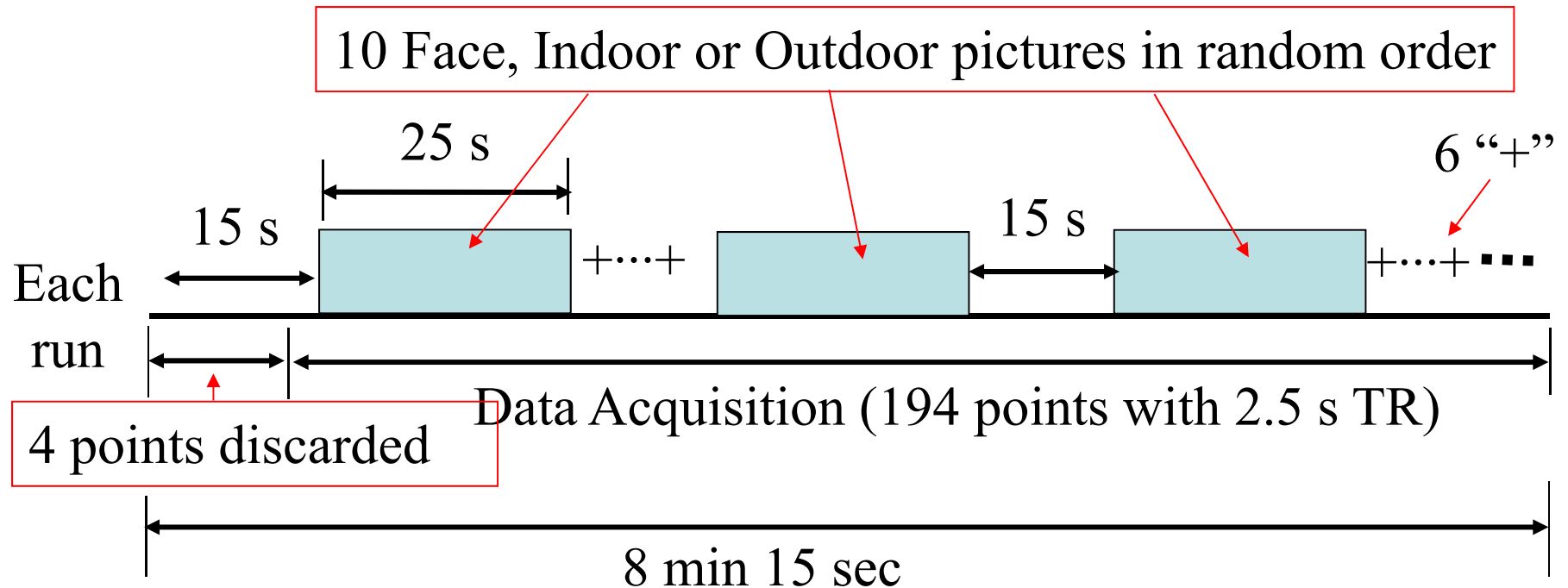
Block design.

4 runs.

Stimuli are randomized.

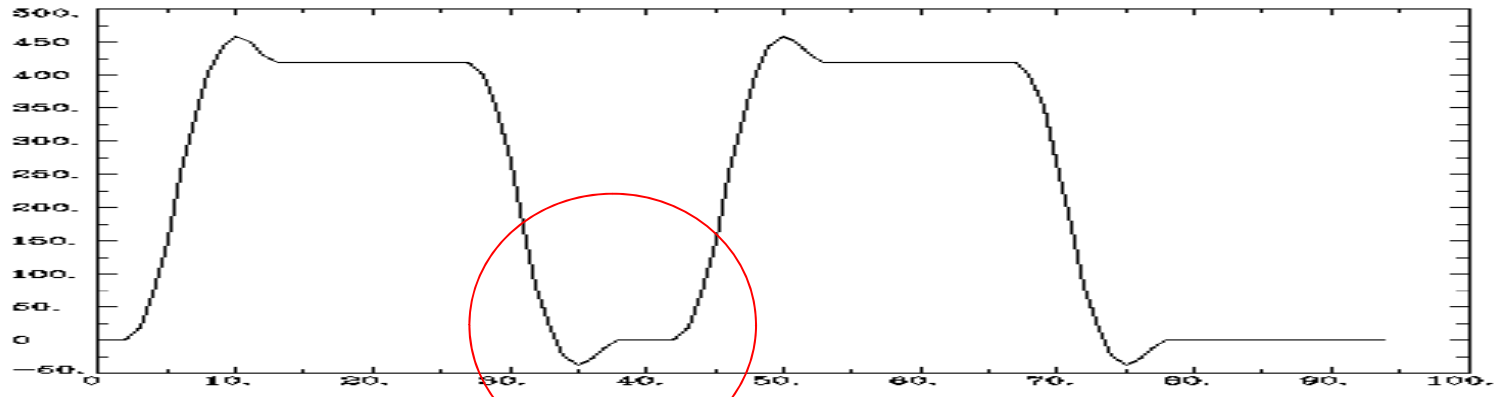
At each run, 6 "+" initial baseline + 12 blocks

At each block, 10 pictures + 6 "+".

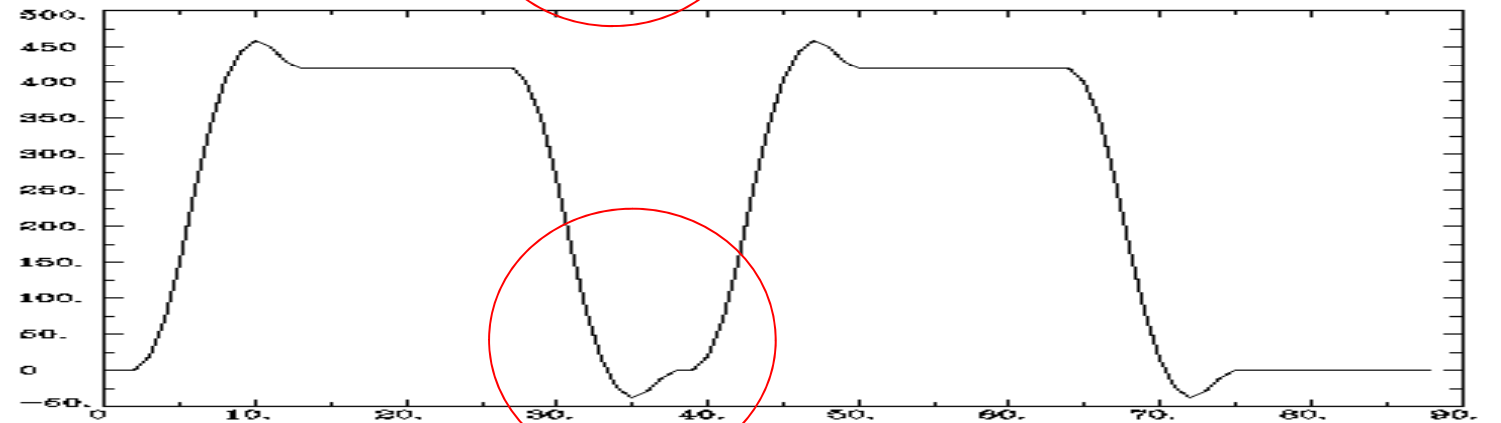


Why choose 15 sec of baseline?

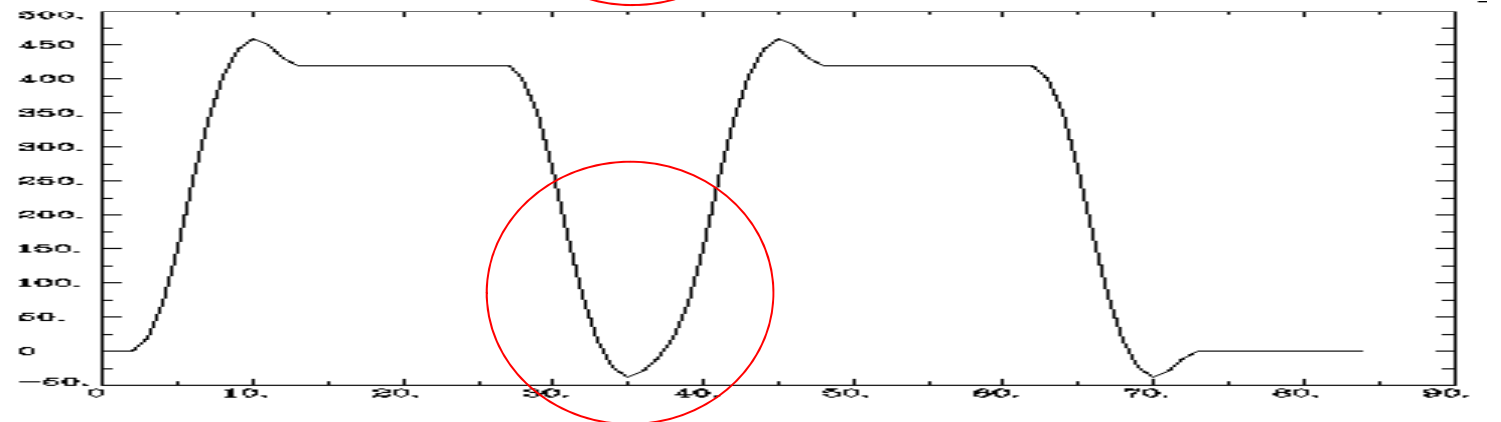
25 sec ON
15 sec OFF



25 sec ON
12 sec OFF

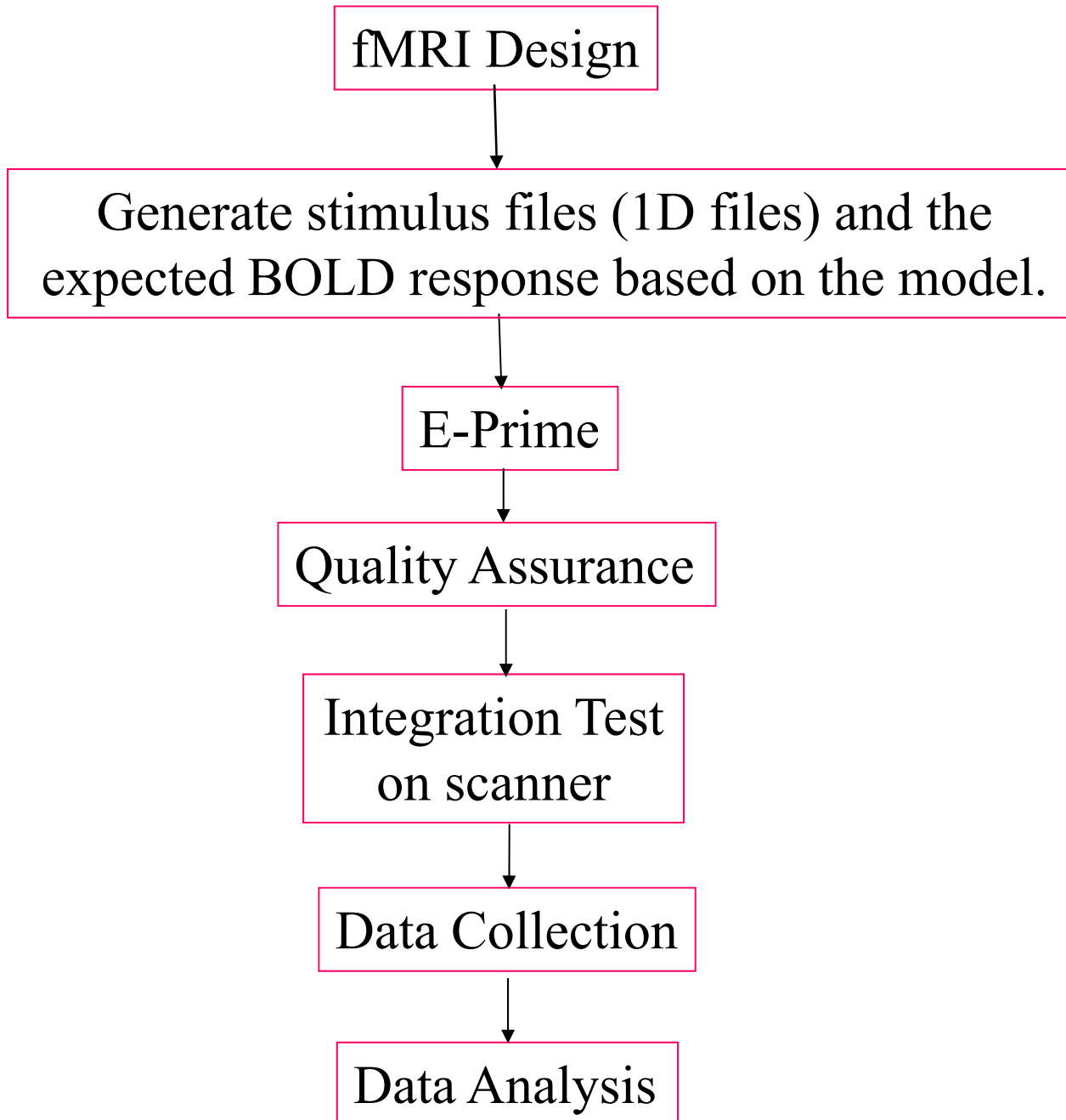


25 sec ON
10 sec OFF



Other considerations: Why choose 25 sec ON and 15 sec OFF?

1. Good duty cycle → shorten the scan time for same detection power.
2. Multiple of TR (2.5 sec).
3. We believe 25 sec is still good for maintaining the attention.



Generate stimulus files (1D files) and the expected BOLD response based on the model.

**Reading Materials:
Chapter 8 and Chapter 10**

Data Analysis

1. Data Pre-processing:

- (1) Registration to AFNI
- (2) Slice timing adjustment
- (3) Motion correction
- (4) Spatial blurring
- (5) Mask generation

2. Data Processing:

- (1) Deconvolution analysis
- (2) Noise analysis (optional)
- (3) Overall significance level
- (4) Group analysis (ANOVA's)
- (5) ROI analysis

Block Design Hand-On

- Scripts to generate a block-design experiment
- Run the script to do the data analysis
- Explain the scripts.

